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### *A categorification of Conway's theory of games (tutorial)*

John Conway, in his theory of two-persons games, constructed an ordered abelian group from the class of all games. The construction depends on the following operations: the sum  $A + B$  of two games  $A$  and  $B$ , the opposite  $-A$  of a game  $A$  and the null game  $0$ . Let us denote by  $W(A)$  the set of winning strategies for the left (player), when the right (player) opens on a game  $A$ . Conway's preorder relation  $A \leq B$  means that  $W(B - A) \neq \emptyset$ . We intend to construct a category whose objects are games, where a morphism  $A \rightarrow B$  is defined an element of  $W(B - A)$ . We recall the notion of compact closed symmetric monoidal category, in which every object has a dual. We would like to show that the category of games is symmetric monoidal and compact. But is it really a category? How do we show that the composition law is associative ? When are two (winning) strategies equivalent? I will address this last question in my afternoon talk.